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Inter. (Part-I)-A- 2015

Roll No.__________ to be filled in by the candidate. (For all sessions)

Paper Code	6	1	9	3

Mathematics (Objective Type)

Time: 30 Minutes **Marks: 20**

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A,B,C & D to each question are given.Which answer you consider correct, fill the corresponding circle A,B,C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. The fraction $\frac{2x^2+5}{x-3}$ is:

(A) proper (B) rational (C) polynomial (D) improper

2. $(n+1)^{th}$ term of an A-P is:

(A) $a_1+(n-1)d$ (B) $a_1-(n-1)d$ (C) a_1+nd (D) a_1-nd

3. Multiplicative inverse of (1 , 0) is:

(A) (-1 , 0) (B) (0 , 1) (C) (0 , -1) (D) (1 , 0)

4. If $a,b\in G$ and G is a group, then $(ab)^{-1}$ is equal to:

(A) $a^{-1}b^{-1}$ (B) $b^{-1}a^{-1}$ (C) $\frac{-1}{ab}$ (D) $\frac{1}{(ab)^{-1}}$

5. If A is a subset of B and A=B then A is:

(A) proper subset of B (B) super set of B (C) improper subset of A (D) proper subset of A

6. Rank of $\begin{bmatrix}1&0&0\\0&1&0\\0&0&0\end{bmatrix}$ is:

(A) 1 (B) 2 (C) 3 (D) 4

7. If A and B are any two non singular matrices then $(AB)^{-1}$ is equal to:

(A) $A^{-1}B^{-1}$ (B) $B^{-1}A^{-1}$ (C) BA (D) AB

8. An equation of the form $ax^2+bx+c=0$ is called quadratic if:

(A) $a=0$ (B) $b=0$ (C) $c=0$ (D) $a\neq 0$

9. The roots of $x^2+2x+3=0$ are:

(A) imaginary (B) real, equal (C) real, unequal (D) rational

10. $\cos^{-1}(-x)$ is equal to:

(A) $\cos^{-1}x$ (B) $\pi+\cos^{-1}x$ (C) $\pi-\cos^{-1}x$ (D) $\sin^{-1}x$

11. Number of solutions of trigonometric equation is:

(A) finite (B) infinite (C) only one (D) all of these

12. The 5th term of sequence 3 , 6 , 12,........ is:

(A) $\frac{1}{48}$ (B) -48 (C) $-\frac{1}{48}$ (D) 48

13. For two events A and B if $P(A)=P(B)=\frac{1}{2}$, then $P(A\cap B)$ is:

(A) $\frac{1}{4}$ (B) $\frac{1}{2}$ (C) 1 (D) Zero

14. $\frac{\lfloor 3}{\lfloor 0}$ equals.

(A) 3 (B) 6 (C) ∞ (D) 12

15. Middle term of $(a+b)^n$, when n is even is:

(A) $\left(\frac{n}{2}+1\right)^{th}$ term (B) $\left(\frac{n}{2}-1\right)^{th}$ term (C) $\frac{n}{2}^{th}$ term (D) $\left(\frac{n}{2}-2\right)^{th}$ term

16. The sum of binomial co-efficients in the expansion of $(1+x)^4$ is:

(A) 8 (B) 10 (C) 16 (D) 32

17. $1+\tan^2\theta$ is equal to:

(A) $\cot\theta$ (B) $\operatorname{cosec}\theta$ (C) $\sec^2\theta$ (D) $-\sec\theta$

18. $\tan\left(3\pi/2-\theta\right)$ is equal to:

(A) $\tan\theta$ (B) $-\cot\theta$ (C) $\cot\theta$ (D) $-\tan\theta$

19. Period of $\tan x/2$ is:

(A) π (B) 2π (C) $\pi/2$ (D) $3\pi/2$

20. In any triangle ABC, with usual notations r_3 is:

(A) $\frac{\Delta}{S-a}$ (B) $\frac{S-b}{\Delta}$ (C) $\frac{S-c}{\Delta}$ (D) $\frac{\Delta}{S-c}$

Roll No.________ *to be filled in by the candidate.*

(For all sessions)

Paper Code	6	0	1	9

Mathematics (Essay Type)

Time: 2:30 Hours **Marks: 80**

Section -I

2. Write short answers of any eight parts from the following. **2x8=16**

i. Prove the rule of addition $\frac{a}{c}+\frac{b}{c}=\frac{a+b}{c}$.

ii. Simplify i^9.

iii. Write any two proper subsets of a set $\{a,b,c\}$.

iv. Define a semi group.

v. Without expansion show that: $\begin{vmatrix} 6 & 7 & 8 \\ 3 & 4 & 5 \\ 2 & 3 & 4 \end{vmatrix}=0$

vi. Evaluate $\left(1+w-w^2\right)^8$

vii. Write the converse and the inverse of the conditional $\sim p \rightarrow q$

viii. For $A=\{1,2,3,4\}$, find a relation $R=\{(x,y)/y=x\}$.

ix. By remainder theorem find remainder when x^2+3x+7 is divided by $x+1$.

x. If A is symmetric or Skew symmetric. Show that A^2 is symmetric.

xi. Find x and y if $\begin{bmatrix} x+3 & 1 \\ -3 & 3y-4 \end{bmatrix}=\begin{bmatrix} 2 & 1 \\ -3 & 2 \end{bmatrix}$.

xii. If α, β be the roots of $x^2-px-p-c=0$, prove that $(1+\alpha)(1+\beta)=1-c$.

3. Write short answers of any eight parts from the following. **2x8=16**

i. Resolve $\frac{1}{x^2-1}$ into partial fractions.

ii. Insert two G.Ms between 2 and 16.

iii. Find the value of n, when ${}^{n}C_{12}={}^{n}C_{6}$.

iv. Evaluate ${}^{9}P_{8}$

v. Expand upto 4 terms $(1-x)^{1/2}$.

vi. Calculate by means of binomial theorem, $(0.97)^3$.

vii. Write the first four terms of the sequence if $a_n=na_{n-1}, a_1=1$.

viii. If 5,8 are two A.Ms between a and b find a and b.

ix. If $\frac{1}{k},\frac{1}{2k+1}$ and $\frac{1}{4k-1}$ are in H.P, find k.

x. Define probability and sample space.

xi. Determine the probability of getting 2 heads in two successive tosses of a balanced coin.

xii. Prove that $1+5+9+........+(4n-3)=n(2n-1)$ for $n=1,2$.

4. Write short answers of any nine parts from the following. **2x9=18**

i. Find r, when $\ell=56cm \quad \theta=45^0$.

ii. Prove that: $\frac{1+\cos\theta}{1-\cos\theta}=(\cos ec\theta+\cot\theta)^2$.

iii. Prove that: $\tan(45^0+A)\tan(45^0-A)=1$.

iv. Prove that: $\frac{\cos 3\theta}{\cos\theta}+\frac{\sin 3\theta}{\sin\theta}=4\cos 2\theta$.

v. Find period of $\operatorname{cosec}\frac{x}{4}$.

vi. Prove that: $\frac{\sin\alpha-\sin\beta}{\sin\alpha+\sin\beta}=\tan\frac{\alpha-\beta}{2}\cot\frac{\alpha+\beta}{2}$.

vii. If α, β, γ are the angles of a triangle ABC, then prove that $\cos(\alpha+\beta)=-\cos\gamma$.

viii. When the angle between the ground and the sun is 30^0, flag pole costs a shadow of 40m long. Find the height of the top of the flag.

ix. Find the measure of greatest angle if the sides of triangle are 16, 20, 33.

x. Find the area of the triangle ABC, if $a=18$, $b=24$, $c=30$.

xi. Show that: $\tan^{-1}(-x)=-\tan^{-1}x$.

xii. Find the solution of the equation $\sin x=-\frac{\sqrt{3}}{2}$ lie in $[0,2\pi]$.

xiii. Find solution of $\sec x=-2$ in $[0,2\pi]$.

Section -II

Note: Attempt any three questions from the following. **10x3=30**

5. (a) Solve the system of linear equation by Cramer's rule $2x+2y+z=3$; $3x-2y-2z=1$; $5x+y-3z=2$.

(b) Solve the equation: $x^{\frac{2}{5}}+8=6x^{\frac{1}{5}}$.

6. (a) Resolve $\frac{4x}{(x+1)^2(x-1)}$ into partial fractions.

(b) If a, b, c, d, are in G.P prove that $a^2-b^2, b^2-c^2, c^2-d^2$ are also in G.P.

7. (a) Two dice are thrown. What is the probability that the sum of the number of dots appearing on them is 4 or 6.

(b) Find the general term in the expansion of $(1+x)^{-3}$, when $|x|<1$.

8. (a) Find the values of trigonometric functions, when $\theta=\frac{13\pi}{3}$. (b) Prove that: $\frac{\cos 8^0-\sin 8^0}{\cos 8^0+\sin 8^0}=\tan 37^0$.

9. (a) Show that: $\gamma=\alpha\sin\frac{\beta}{2}\sin\frac{\gamma}{2}\sec\frac{\alpha}{2}$. (b) Prove that: $2\tan^{-1}\frac{1}{3}+\tan^{-1}\frac{1}{7}=\frac{\pi}{4}$.

Roll No.________ to be filled in by the candidate. **(For all sessions)**

Paper Code	6	1	9	1

Mathematics (Objective Type)

Time: 30 Minutes **Marks: 20**

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A,B,C & D to each question are given. Which answer you consider correct, fill the corresponding circle A,B,C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. If Z is a complex number, then $|Z|^2$ is:

(A) Z^2 (B) $(\overline{Z})^2$ (C) $Z\overline{Z}$ (D) $\frac{Z}{\overline{Z}}$

2. For any two sets A and B, $(A\cap B)'$ is equal to:

(A) A' (B) B' (C) $A'\cup B'$ (D) $A\cap B$

3. The multiplicative identity in the set of real numbers is:

(A) Zero (B) 1 (C) 3 (D) 2

4. A square matrix $A=[aij]$ with complex entries is called skew Hermitian if $(\overline{A})^t$ is equal to:

(A) A (B) -A (C) $|A|$ (D) $-|A|$

5. If A and B are any two non singular matrices such that $(AB)^{-1}$ is equal to:

(A) $A^{-1}B^{-1}$ (B) $B^{-1}A^{-1}$ (C) BA (D) AB

6. A reciprocal equation remains unchanged when variable x is replaced by:

(A) $\frac{1}{x}$ (B) $\frac{-1}{x}$ (C) $\frac{1}{x^2}$ (D) $-x$

7. The roots of equation $x^2-5x+6=0$ are:

(A) 2 , -3 (B) -2 , -3 (C) 2 , 3 (D) -2 , 3

8. $(x-1)^2=x^2-2x+1$ is called:

(A) equation (B) conditional (C) identity (D) fraction

9. A.M between $3\sqrt{5}$ and $5\sqrt{5}$ is:

(A) $4\sqrt{5}$ (B) $5\sqrt{5}$ (C) 10 (D) $2\sqrt{5}$

10. n^{th} term of G.P is:

(A) $a_1\gamma^n$ (B) $a_1\gamma^{n-1}$ (C) $\frac{a}{r^n}$ (D) $\frac{r^n}{a}$

11. If $n=1$, then value of $n\underline{|n-1}$ is:

(A) Zero (B) 1 (C) 2 (D) -1

12. $\overset{n}{\underset{0}{C}}$ equals.

(A) 1 (B) n (C) zero (D) 2

13. General term of expansion $(a+x)^n$ is:

(A) $\binom{n+1}{r}a^{n-r}x^r$ (B) $\binom{n}{r-1}a^{n-r}x^r$ (C) $\binom{n}{r+1}a^r x^{n-r}$ (D) $\binom{n}{r}a^{n-r}x^r$

14. The sum of binomial co-efficients in the expansion of $(1+x)^4$ is:

(A) 8 (B) 10 (C) 16 (D) 32

15. $\cos^2 2\theta+\sin^2 2\theta$ is equal to:

(A) 1 (B) zero (C) $\sec^2\theta$ (D) 2

16. $\cos\left(\pi/2-\beta\right)$ is equal to:

(A) $\sin\beta$ (B) $-\sin\beta$ (C) $\cos\beta$ (D) $-\cos\beta$

17. Period of $\cos ec10x$ is:

(A) $\frac{\pi}{10}$ (B) $\frac{2\pi}{5}$ (C) $\frac{\pi}{5}$ (D) $\frac{4\pi}{5}$

18. For any triangle ABC, with usual notations r_2 is equal to:

(A) $\frac{\Delta}{S-a}$ (B) $\frac{\Delta}{S-c}$ (C) $\frac{\Delta}{S-b}$ (D) $\frac{\Delta}{S}$

19. $\tan\left(\sin^{-1}x\right)$ is equal to:

(A) $1+2x^2$ (B) $1-x^2$ (C) $\frac{x}{\sqrt{1-x^2}}$ (D) $\frac{2x}{\sqrt{1+x^2}}$

20. The solutions of equation $\frac{1}{2}+\sin\theta=0$ are in quadrant.

(A) I & IV (B) I & III (C) III & IV (D) II & IV

Roll No. ________ to be filled in by the candidate.	(For all sessions)	Paper Code	6	0	1	9

Mathematics (Essay Type)

Time: 2:30 Hours **Marks: 80**

Section -I

2. Write short answers of any eight parts from the following. **2x8=16**

i. Find the multiplicative inverse of (-4 , 7).

ii. Find real and imaginary parts of $\left(\sqrt{3}+i\right)^3$.

iii. Define equivalent sets.

iv. Define monoid.

v. Find the inverse of the matrix $A=\begin{bmatrix} 3 & -1 \\ 2 & 1 \end{bmatrix}$.

vi. Show that $\begin{vmatrix} 1 & 2 & 3x \\ 2 & 3 & 6x \\ 3 & 5 & 9x \end{vmatrix}=0$, without expansion.

vii. Find the value of λ if $A=\begin{bmatrix} 4 & \lambda & 3 \\ 7 & 3 & 6 \\ 2 & 3 & 1 \end{bmatrix}$ is singular.

viii. Define exponential equation.

ix. If $U=\{1,2,3,.........,10\}$, $A=\{2,4,6,........,20\}$ and $B=\{1,3,5,......,19\}$, prove that $(A\cup B)'=A'\cap B'$.

x. Write converse and contrapositive of the conditional $Nq \rightarrow Np$.

xi. Find three cube-cube roots of unity.

xii. If α,β are the roots of $3x^2-2x+4=0$, find the values of $\frac{1}{\alpha^2}+\frac{1}{\beta^2}$.

3. Write short answers of any eight parts from the following. **2x8=16**

i. Resolve $\frac{1}{(x-1)(2x-1)}$ into partial fractions.

ii. Which term of the A.P 5,2,-1....is -85.

iii. Find the value of n if ${}^{n}P_{4} : {}^{n-1}P_{3} = 9:1$.

iv. Find the number of diagonals of 12 sided figure.

v. Find the first four terms of $(1+2x)^{-1}$.

vi. Find the 6th term in the expansion of $\left(x^2-\frac{3}{2x}\right)^{10}$.

vii. Find the next two terms of the sequence 1 , -3 , 5 , -7 , 9 , -11............

viii. If 5,8 are two A.Ms between a and b find a and b.

ix. Convert the recurring decimal $2.\dot{2}\dot{3}$ into the equivalent common fraction.

x. Convert $n(n-1)(n-2)......(n-r+1)$ in the factorial form.

xi. How many numbers greater than 1000,000 can be formed from digits 0 , 2 , 2 , 2 , 3 , 4 , 4.

xii. Show that inequality $4^n > 3^n + 4$ is true for $n=2,3$.

4. Write short answers of any nine parts from the following. **2x9=18**

i. Verify $2\sin 45^0+\frac{1}{2}co\sec 45^0=\frac{3}{\sqrt{2}}$.

ii. Prove that: $\cot^2\theta-\cos^2\theta=\cot^2\theta\cos^2\theta$.

iii. Find the value of $\tan 75^0$ (without calculator).

iv. Prove that: $\cos 306^0+\cos 234^0+\cos 162^0+\cos 18^0=0$.

v. Prove that $\sqrt{\dfrac{1+\sin\alpha}{1-\sin\alpha}}=\dfrac{\sin\alpha/2+\cos\alpha/2}{\sin\alpha/2-\cos\alpha/2}$.

vi. Prove that: $\sin\left(\dfrac{\pi}{4}-\theta\right)\sin\left(\dfrac{\pi}{4}+\theta\right)=\dfrac{1}{2}\cos 2\theta$.

vii. Find the period of $\operatorname{cosec} x/4$.

viii. Show that: $\tan\left(\sin^{-1}x\right)=\dfrac{x}{\sqrt{1-x^2}}$.

ix. Prove that $abc\left(\sin\alpha+\sin\beta+\sin\gamma\right)=4\Delta S$.

x. Define trigonometric equation.

xi. Find the area of triangle ABC, if $a=524$, $b=276$, $c=315$.

xii. Find the smallest angle of the triangle ABC, when $a=37.34$, $b=3.24$, $c=35.06$.

xiii. Find the solution of $\sec x=-2$ which lies in $\left[0,2\pi\right]$.

Section -II

Note: Attempt any three questions from the following. **10x3=30**

5. (a) Use Cramer's rule to solve the system $2x+2y+z=3$; $3x-2y-2z=1$; $5x+y-3z=2$.

(b) If α and β are the roots of $x^2-3x+5=0$ form the equation whose roots are $\dfrac{1-\alpha}{1+\alpha}$ and $\dfrac{1-\beta}{1+\beta}$.

6. (a) Resolve into partial fractions. $\dfrac{x^2}{(x-1)^2(x+1)}$.

(b) For what value of n $\dfrac{a^n+b^n}{a^{n-1}+b^{n-1}}$ is G.M between a and b.

7. (a) How many arrangements of the letters of the word ATTACKED can be made

if each arrangement begins with C and ends with K.

(b) Find the co-efficient of x^5 in the expansion of $\left(x^2-\dfrac{3}{2x}\right)^{10}$.

8. (a) Prove the identity $\sin^6\theta-\cos^6\theta=\left(\sin^2\theta-\cos^2\theta\right)\left(1-\sin^2\theta\cos^2\theta\right)$.

(b) If $\sin\alpha=\dfrac{4}{5}$ and $\cos\beta=\dfrac{40}{41}$ where $0<\alpha<\pi/2$ and $0<\beta<\pi/2$ show that $\sin\left(\alpha-\beta\right)=\dfrac{133}{205}$.

9. (a) The sides of a triangle are x^2+x+1, $2x+1$ and x^2-1 prove that the greater angle of the triangle is 120^0.

(b) Prove that $\tan^{-1}\dfrac{1}{11}+\tan^{-1}\dfrac{5}{6}=\tan^{-1}\dfrac{1}{3}+\tan^{-1}\dfrac{1}{2}$.

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Inter. (Part-I)-A- 2017

Roll No.__________ *to be filled in*

(For all sessions)

Paper Code	6	1	9	1

Mathematics (Objective Type) Group-I

Time: 30 Minutes **Marks: 20**

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A,B,C & D to each question are given.Which answer you consider correct, fill the corresponding circle A,B,C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. $\overline{-a-ib}$ equals:

(A) $a+ib$ (B) $-a+ib$ (C) $a-ib$ (D) $-a-ib$

2. w^3 equals:

(A) 0 (B) -1 (C) i (D) 1

3. Sum of complex roots of unity equals:

(A) 0 (B) -1 (C) 1 (D) w

4. $(z,+)$ has no identity other than:

(A) 1 (B) -1 (C) i (D) 0

5. $(AB)^{-1}$ equals:

(A) $A^{-1}B^{-1}$ (B) A^{-1} (C) B^{-1} (D) $B^{-1}A^{-1}$

6. [8] is a:

(A) square matrix (B) unit matrix (C) scalar matrix (D) rectangular matrix

7. Partial fractions of $\frac{x^2+1}{(x+1)(x-1)}$ will be of the form:

(A) $\frac{A}{x+1}+\frac{B}{x-1}$ (B) $\frac{Ax+B}{x+1}+\frac{C}{x-1}$ (C) $1+\frac{A}{x+1}+\frac{B}{x-1}$ (D) $\frac{Ax+B}{x^2-1}$

8. G.M between $2i$ and $8i$ equals:

(A) ± 4 (B) 4 (C) -4 (D) $\pm 4i$

9. No term in G.P is:

(A) 3 (B) 2 (C) 1 (D) 0

10. A die is rolled then n(s) equals:

(A) 36 (B) 6 (C) 1 (D) 9

11. The factorial form of 6.5.4 is:

(A) $\frac{6!}{3!}$ (B) $6!$ (C) $3!$ (D) $\frac{6!}{2!}$

12. In the expansion of $(3+x)^4$ middle term will be:

(A) 81 (B) $54x^2$ (C) $26x^2$ (D) x^4

13. The sum of odd coefficients in the expansion of $(1+x)^5$ is:

(A) 16 (B) 32 (C) 25 (D) 5

14. One radian equals:

(A) 45^0 (B) 50^0 (C) 60^0 (D) 57.296^0

15. $\sin\theta$ equals:

(A) $2\sin^2 \theta/2$ (B) $2\sin\theta/2 \cos\theta/2$ (C) $2\cos^2 \theta/2$ (D) $2\tan\theta/2$

16. Period of $\tan x/3$ is:

(A) π (B) 2π (C) 3π (D) $\pi/2$

17. Number of elements of a triangle are:

(A) 3 (B) 4 (C) 6 (D) 8

18. Radius of inscribed circle is:

(A) $\frac{\Delta}{S}$ (B) $\frac{S}{\Delta}$ (C) $\frac{\Delta}{S-c}$ (D) $\frac{4\Delta}{abc}$

19. $2\tan^{-1} A$ equals:

(A) $\tan^{-1}\left(\frac{A}{1-A^2}\right)$ (B) $\tan^{-1}\left(\frac{2A}{1+A^2}\right)$ (C) $\tan^{-1}\left(\frac{-2A}{1+A^2}\right)$ (D) $\tan^{-1}\left(\frac{2A}{1-A^2}\right)$

20. If $\cos x = \frac{\sqrt{3}}{2}, x \in [0,\pi]$, then x equals:

(A) $\frac{-\pi}{6}$ (B) $\frac{5\pi}{6}$ (C) $\frac{\pi}{6}$ (D) $\frac{7\pi}{6}$

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Roll No.__________ *to be filled in by the candidate.*

(For all sessions)

Mathematics (Essay Type) Group-I

Time: 2:30 Hours **Marks: 80**

Section -I

2. Write short answers of any eight parts from the following. **2x8=16**

i. Show that $\forall z \in c \; z^2 + z^{-2}$ is a real number.

ii. Simplify by justifying each step $\dfrac{\frac{1}{a}-\frac{1}{b}}{1-\frac{1}{a}.\frac{1}{b}}$.

iii. Write down the power set of { 9,11}.

iv. Solve by using quadratic formula $15x^2 + 2ax - a^2 = 0$

v. Convert $(A \cap B)' = A' \cup B'$ into logic form.

vi. If a, b are elements of a group G, solve $ax = b$.

vii. Show that $\begin{vmatrix} 2 & 3 & 0 \\ 3 & 9 & 6 \\ 2 & 15 & 1 \end{vmatrix} = 9\begin{vmatrix} 2 & 1 & 0 \\ 1 & 1 & 2 \\ 2 & 5 & 1 \end{vmatrix}$

viii. Prove that $\left(\dfrac{1+\sqrt{-3}}{2}\right)^9 + \left(\dfrac{1-\sqrt{-3}}{2}\right)^9 = -2$.

ix. Simplify $(5,-4) \div (-3,-8)$.

x. If $A = \begin{bmatrix} 1 & 2 \\ a & b \end{bmatrix}$ and $A^2 = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$, find the values of a and b.

xi. If the matrices A and B are symmetric and AB=BA. Show that AB is symmetric.

xii. Show that roots of $(p+q)x^2 - px - q = 0$ are rational.

3. Write short answers of any eight parts from the following. **2x8=16**

i. Resolve $\dfrac{1}{x^2-1}$ into partial fractions.

ii. Find next two terms of sequence -1,2,12,40,........

iii. Find A.M between $x-3$ and $x+5$.

iv. Write 8.7.6.5 in the factorial form.

v. Evaluate $^{12}P_5$.

vi. If $^nC_8 = {^nC_{12}}$ find n.

vii. Find vulgar fraction equivalent to 0.7^0 recurring decimal.

viii. If the numbers $\dfrac{1}{k}, \dfrac{1}{2k+1}$ and $\dfrac{1}{4k-1}$ are in Harmonic sequence, find k.

ix. Determine the probability of getting 2 heads in two successive tosses of a balanced coin.

x. Show that $4^n > 3^n + 4$ is not true for $n = 1$.

xi. Calculate $(2.02)^4$ by means of binomial theorem.

xii. Expand $(1+2x)^{-1}$ upto four terms.

4. Write short answers of any nine parts from the following. **2x9=18**

i. Convert $18^0 6' 21''$ to decimal form.

ii. Prove that: $\cos^2\theta - \sin^2\theta = \cos^4\theta - \sin^4\theta$.

iii. Find the value of $\tan 105^0$ (without calculator).

iv. Prove that: $\dfrac{\sin 3x - \sin x}{\cos x - \cos 3x} = \cot 2x$.

v. Find the value of $\sec(-300^0)$ (without table).

vi. Find the domain and range of $\sec x$.

vii. Define angle of elevation.

viii. The area of triangle is 2437 and $a=79, c=97$, find β.

ix. Show that $\tan(\sin^{-1}x)=\dfrac{x}{\sqrt{1-x^2}}$.

x. Define trigonometric equation.

xi. Verify $\sin^2\dfrac{\pi}{6}:\sin^2\dfrac{\pi}{4}:\sin^2\dfrac{\pi}{3}:\sin^2\dfrac{\pi}{2}=1:2:3:4$.

xii. A kite is flying at a height of 67.2m is attached to a fully stretched string inclined at an angle of 55^0 to the horizontal. Find the length of the string.

xiii. Solve $\sin x+\cos x=0$, where x lies in $[0,2\pi]$.

Section -II

Note: Attempt any three questions from the following. **10x3=30**

5. (a) If $A=\begin{bmatrix} i & 1+i \\ 1 & -i \end{bmatrix}$, show that $A+(\overline{A})^t$ is Hermitian.

(b) If the roots of $px^2+qx+q=0$, are α and β, then prove that $\sqrt{\alpha/\beta}+\sqrt{\beta/\alpha}+\sqrt{q/p}=0$

6. (a) Resolve $\dfrac{x^2}{(x-2)(x-1)^2}$ into partial fractions.

(b) Insert five Harmonic means between $\dfrac{1}{4}$ and $\dfrac{1}{24}$.

7. (a) Find the value of n and r, when ${}^nC_r=35$ and ${}^nP_r=210$.

(b) Identify the series $1+\dfrac{1}{3}+\dfrac{1}{3.6}+\dfrac{1}{3.6.9}+\dots\dots\dots\dots$ as a Binomial expansion and find its sum.

8. (a) If $\operatorname{cosec}\theta=\dfrac{m^2+1}{2m}$ and $m>0, \left(0<\theta<\dfrac{\pi}{2}\right)$ find the values of the remaining trigonometric ratios.

(b) Reduce $\sin^4\theta$ to an expression involving only function of multiples of θ, raised to the first power.

9. (a) Solve the triangle using first law of tangent and then law of sines $a=319$, $b=168$, $r=110^0 22'$.

(b) Prove that $\sin^{-1}\dfrac{77}{85}-\sin^{-1}\dfrac{3}{5}=\cos^{-1}\dfrac{15}{17}$.

☆ (3)

Inter. (Part-I)-A- 2017

Roll No.__________ to be filled in by the candidate.	(For all sessions)	Paper Code	6	1	9	2

Mathematics (Objective Type) Group-II

Time: 30 Minutes **Marks: 20**

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A,B,C & D to each question are given.Which answer you consider correct, fill the corresponding circle A,B,C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. $\left|-\frac{1}{2}+\frac{\sqrt{3}}{2}i\right|$ equals:

(A) 3 (B) 2 (C) 1 (D) zero

2. If a and b are elements of a group G, then $(ab)^{-1}$ equals:

(A) $a^{-1}b^{-1}$ (B) $b^{-1}a^{-1}$ (C) $a^{-1}b$ (D) $b^{-1}a$

3. For any non-singular matrix A, A^{-1} equals:

(A) $\frac{adjA}{A}$ (B) $\frac{adjA}{|A|}$ (C) $\frac{|A|}{adjA}$ (D) $|A|.adjA$

4. A square matrix A is said to be Hermitian if:

(A) $(\overline{A})^t = A$ (B) $(\overline{A})^t = -A$ (C) $(\overline{A})^t = -\overline{A}$ (D) $(\overline{A})^t = \overline{A}$

5. If α, β are the roots of $4x^2+5x-6=0$, then value of $4\alpha+4\beta$ equals:

(A) $-5/4$ (B) -5 (C) -6 (D) 5

6. If w is cube root of unity, then $1+w^{28}+w^{29}$ equals:

(A) 1 (B) zero (C) w (D) w^2

7. The partial fraction of $\frac{1}{(x+1)(x^2-1)}$ will be of the form:

(A) $\frac{A}{x+1}+\frac{Bx+C}{x^2-1}$ (B) $\frac{A}{x+1}+\frac{B}{(x+1)^2}+\frac{C}{x-1}$ (C) $\frac{A}{x^2-1}+\frac{B}{x+1}$ (D) $\frac{A}{x+1}+\frac{B}{x^2-1}$

8. Arithmetic Mean between two numbers $\frac{1}{a}$ and $\frac{1}{b}$ is:

(A) $\frac{a+b}{2}$ (B) $\frac{2}{a+b}$ (C) $\frac{a+b}{2ab}$ (D) $\frac{2ab}{a+b}$

9. If A, G, H have their usual meanings and a and b are positive distinct real numbers and $G>0$, then

(A) $A<G<H$ (B) $A>G>H$ (C) $A<H<G$ (D) $A>H>G$

10. If A and B are disjoint events, then $p(A \cup B)$ equals:

(A) $P(A)+P(B)$ (B) $P(A)+P(B)-P(A \cap B)$ (C) $P(A)+P(B)+P(A \cap B)$ (D) $P(A)-P(B)$

11. If two dice are thrown simultaneously, then the number of elements in the sample space are:

(A) 6 (B) 12 (C) 24 (D) 36

12. The number of terms in the expansion of $(1+x)^{1/2}, |x|<1$ are:

(A) 2 (B) n (C) $\frac{n}{2}$ (D) infinite

13. If n is positive integer , then $n^2 > n+3$ is true when:

(A) $n \geq 3$ (B) $n \geq 2$ (C) $n \geq 1$ (D) $n \leq 3$

14. $\cot^2\theta - \cos ec^2\theta$ equals:

(A) 1 (B) -1 (C) $\cot\theta$ (D) $\cos ec\theta$

15. $\frac{3\pi}{2}+\theta$ lies in:

(A) 1st quadrant (B) 2nd quadrant (C) 3rd quadrant (D) 4th quadrant

16. Period of $\cos\frac{x}{2}$ is:

(A) π (B) 2π (C) 4π (D) $\frac{\pi}{2}$

17. With usual notaions, in any triangle ABC, if $\Delta = 20$ a=4 , b=6 , c=10, then r equals:

(A) 2 (B) 5 (C) 10 (D) 15

18. $\sin\left(\sin^{-1}\left(\frac{1}{2}\right)\right)$ equals:

(A) $\frac{\pi}{3}$ (B) $\frac{\pi}{6}$ (C) $\frac{1}{2}$ (D) $\frac{\sqrt{3}}{2}$

19. With usual notations, r_1 equals:

(A) $\frac{\Delta}{s}$ (B) $\frac{\Delta}{s-a}$ (C) $\frac{\Delta}{s-b}$ (D) $\frac{\Delta}{s-c}$

20. If $\sin x = -\frac{\sqrt{3}}{2}$, then refrence angle is:

(A) $\frac{\pi}{6}$ (B) $-\frac{\pi}{6}$ (C) $\frac{\pi}{3}$ (D) $-\frac{\pi}{3}$

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Roll No.________ *to be filled in by the candidate.*

(For all sessions)

Mathematics (Essay Type) Group-II

Time: 2:30 Hours **Marks: 80**

Section -I

2. Write short answers of any eight parts from the following. **2x8=16**

i. Simplify $(a+ib)^3$.

ii. If B={1,2,3}, find the power set of B.

iii. Define the conjunction.

iv. Define the identity martix.

v. If $z=a+ib$ show that $(z-\bar{z})^2$ is real number.

vi. Show that $x^3+y^3=(x+y)(x+wy)(x+w^2y)$.

vii. Evaluate the determinent of $A=\begin{bmatrix}1 & -2 & 3\\ 2 & 3 & 1\\ 4 & -3 & 2\end{bmatrix}$.

viii. If $A=\begin{bmatrix}1 & -1\\ a & b\end{bmatrix}$ and $A^2=\begin{bmatrix}1 & 0\\ 0 & 1\end{bmatrix}$ find the values of a and b.

ix. Does the set $\{0,-1\}$ have closure property w.r.t addition and multiplication?

x. Solve the equation by completing square $x^2-3x-648=0$.

xi. If a, b are elements of a group G, then show that $(ab)^{-1}=b^{-1}a^{-1}$.

xii. If α,β are the roots of the equation $3x^2-2x+4=0$, find the values of $\frac{\alpha}{\beta}+\frac{\beta}{\alpha}$.

3. Write short answers of any eight parts from the following. **2x8=16**

i. Define proper rational fraction.

ii. Write next two terms of -1,2,12,40,............

iii. If $S_n=n(2n-1)$, then find the series.

iv. Insert two G.Ms between 1 and 8.

v. Expand $(1-x)^{1/2}$ upto 4 terms.

vi. Prove that ${}^{n}C_{r}={}^{n}C_{n-r}$.

vii. How many 5-digit multiples of 5 can be formed from the digits 2,3,5,7,9 (no digit repeated).

viii. Determine the probability of getting 2 heads in two successive tosses of a balanced coin.

ix. A die is rolled. Find the probability that the dots on top are prime numbers or odd numbers.

x. Show that $1+5+9+......+(4n-3)=n(2n-1)$ is true for $n=1$ and $n=2$.

xi. Using binomial theorem find the value of $\sqrt{99}$.

xii. Find the General term of $\left(\frac{a}{2}-\frac{2}{a}\right)^6$.

4. Write short answers of any nine parts from the following. **2x9=18**

i. Convert $54^0 45'$ into radians.

ii. Find x, if $\tan^2 45^0-\cos^2 60^0=x\sin 45^0\cos 45^0\tan 60^0$.

iii. Prove that: $\frac{1}{1+\sin\theta}+\frac{1}{1-\sin\theta}=2\sec^2\theta$.

iv. Prove that: $\cot(\alpha+\beta)=\frac{\cot\alpha\cot\beta-1}{\cot\alpha+\cot\beta}$.

v. Find the value of $\sin 105^0$.

vi. Express $\cos(x+y)\sin(x-y)$ as sum or difference.

vii. Find the period of $\sin \frac{x}{5}$.

viii. State the law of cosine.

ix. Show that: $\frac{1}{r}=\frac{1}{r_1}+\frac{1}{r_2}+\frac{1}{r_3}$.

x. Find domain and range of $y=\cos^{-1}x$.

xi. Solve the equation $1+\cos x=0$.

xii. Find the solution of $\sec x=-2$, $x\in[0,2\pi]$.

xiii. Find the area of the triangle ABC in which a=18 , b=24 , c=30.

Section -II

Note: Attempt any three questions from the following. **10x3=30**

5. (a) Show that $\begin{vmatrix} a+\lambda & b & c \\ a & b+\lambda & c \\ a & b & c+\lambda \end{vmatrix}=\lambda^2(a+b+c+\lambda)$

(b) If α and β are the roots of $5x^2-x-2=0$ form the equation roots are $\frac{3}{\alpha}$ and $\frac{3}{\beta}$.

6. (a) Resolve $\frac{1}{(x-3)^2(x+1)}$ into partial fractions.

(b) If the (Positive) G.M and H.M between two numbers are 4 and $\frac{16}{5}$, find the numbers.

7. (a) How many numbers greater than one million can be formed from the digits 0,2,2,2,3,4,4?

(b) Find the co-efficient of the term involving x^{-1} in the expansion of $\left(\frac{3x}{2}-\frac{1}{3x}\right)^{11}$.

8. (a) Prove that: $\frac{\tan\theta+\sec\theta-1}{\tan\theta-\sec\theta+1}=\tan\theta+\sec\theta$.

(b) Prove that: $\frac{\sin\alpha-\sin\beta}{\sin\alpha+\sin\beta}=\tan\frac{\alpha-\beta}{2}\cot\frac{\alpha+\beta}{2}$.

9. (a) Prove that in an equilateral triangle $r:R:r_1=1:2:3$.

(b) Prove that $\sin^{-1}\frac{5}{13}+\sin^{-1}\frac{7}{25}=\cos^{-1}\frac{253}{325}$.

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Roll No.____________ *to be filled in by the candidate.*

(For all sessions)

Paper Code	6	1	9	5

Mathematics (Objective Type)

Time: 30 Minutes **Marks: 20**

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A,B,C & D to each question are given.Which answer you consider correct, fill the corresponding circle A,B,C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. If n is a positive even integer, then $\binom{n}{1}+\binom{n}{3}+\binom{n}{5}+\dots\dots+\binom{n}{n-1}$ is equal to:

(A) 2^n (B) 2^{n+1} (C) 2^{n-1} (D) 3^n

2. An angle in the standard position whose terminal side falls on $x-$axis or $y-$axis is:

(A) General angle (B) coterminal angle (C) Quadrantal angle (D) acute angle

3. $\cos(\pi+\theta)$ is equal to:

(A) $\sec\theta$ (B) $-\cos\theta$ (C) $\cos\theta$ (D) $-\sec\theta$

4. Range of Cosine function is:

(A) $(-1,1)$ (B) $[-1,1]$ (C) $[-1,1)$ (D) $(-1,1]$

5. In any $\triangle ABC$ $rr_1r_2r_3 =$ _______

(A) Δ^4 (B) Δ^3 (C) Δ^2 (D) Δ

6. With usual notation $\sqrt{\dfrac{(s-b)(s-c)}{bc}}$ is equal to:

(A) $\cos\dfrac{\alpha}{2}$ (B) $\sin\dfrac{\alpha}{2}$ (C) $\sin\dfrac{\beta}{2}$ (D) $\sin\dfrac{\gamma}{2}$

7. $\cos^{-1}(-x)$ is equal to:

(A) $\dfrac{\pi}{2}-\sin^{-1}x$ (B) $\dfrac{\pi}{2}+\sin^{-1}x$ (C) $\pi+\cos^{-1}x$ (D) $\pi-\cos^{-1}x$

8. Solution of the equation $\tan x+1=0$ is:

(A) $\left\{\dfrac{3\pi}{4}+n\pi\right\}$ (B) $\left\{\dfrac{\pi}{4}+n\pi\right\}$ (C) $\{\pi+n\pi\}$ (D) $\{2\pi+n\pi\}$, when $n\in z$

9. If $z=a+ib$, what is the value of $\cos\theta$?

(A) $\dfrac{a}{|z|}$ (B) $\dfrac{b}{|z|}$ (C) $\dfrac{a}{b}$ (D) $\dfrac{b}{a}$

10. A function $f: A \to B$ is surjective if:

(A) Range $f = A$ (B) Range $f = B$ (C) Range $f \neq B$ (D) Range $f \neq A$

11. Determinant of any unit matrix has value:

(A) Greater than 1 (B) less than 1 (C) 1 (D) zero

12. A square matrix A is skew -symmetric if A^t is equal to:

(A) A (B) -A (C) A^t (D) A^2

13. The discriminant of $ax^2 + bx + c = 0$, $a \neq 0$ is:

(A) $b^2 + 4ac$ (B) $4ac - b^2$ (C) $b^2 - 4ac$ (D) $a^2 - 4ac$

14. The degree of the equation $x^3 + 3x^2 + 4x + 5 = 0$ is

(A) 4 (B) 3 (C) 2 (D) 1

15. $\frac{x^2+1}{Q(x)}$ will be improper fraction if

(A) Degree of $Q(x) = 2$ (B) Degree of $Q(x) = 3$

(C) Degree of $Q(x) = 4$ (D) Degree of $Q(x) = 5$

16. $\sum_{K=1}^{n} K$ is equal to:

(A) $\frac{n+1}{2}$ (B) $\frac{n}{2}$ (C) $\frac{n(n+1)}{2}$ (D) $\frac{n(n-1)}{2}$

17. The geometric mean between $-2i$ and $8i$ is:

(A) ± 1 (B) ± 2 (C) ± 3 (D) ± 4

18. If A and B are mutually exclusive events, then $P(A \cup B)$ is equal to:

(A) $P(A) + P(B)$ (B) $P(A) - P(B)$ (C) $P(AB)$ (D) $P(A) \cap P(B)$

19. If ${}^{n}C_{8} = {}^{n}C_{12}$, then n is equal to:

(A) 8 (B) 12 (C) 20 (D) 0

20. In the expansion of $(x+y)^8$, middle term is:

(A) T_4 (B) T_6 (C) T_3 (D) T_5

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Inter. (Part-I)-A- 2018

Roll No.________ to be filled in by the candidate.	(For all sessions)	Paper Code	6	1	9	7

Mathematics (Objective Type)

Time: 30 Minutes **Marks: 20**

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A,B,C & D to each question are given.Which answer you consider correct, fill the corresponding circle A,B,C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. The geometric mean between $-2i$ and $8i$ is:

(A) ± 1 (B) ± 2 (C) ± 3 (D) ± 4

2. If A and B are mutually exclusive events, then $P(A \cup B)$ is equal to:

(A) $P(A)+P(B)$ (B) $P(A)-P(B)$ (C) $P(AB)$ (D) $P(A) \cap P(B)$

3. If ${}^{n}C_{8} = {}^{n}C_{12}$, then n is equal to:

(A) 8 (B) 12 (C) 20 (D) 0

4. In the expansion of $(x+y)^8$, middle term is:

(A) T_4 (B) T_6 (C) T_3 (D) T_5

5. If n is a positive even integer, then $\binom{n}{1}+\binom{n}{3}+\binom{n}{5}+\dots\dots+\binom{n}{n-1}$ is equal to:

(A) 2^n (B) 2^{n+1} (C) 2^{n-1} (D) 3^n

6. An angle in the standard position whose terminal side falls on x-axis or y-axis is:

(A) General angle (B) coterminal angle (C) Quadrantal angle (D) acute angle

7. $\cos(\pi+\theta)$ is equal to:

(A) $\sec\theta$ (B) $-\cos\theta$ (C) $\cos\theta$ (D) $-\sec\theta$

8. Range of Cosine function is:

(A) $(-1,1)$ (B) $[-1,1]$ (C) $[-1,1)$ (D) $(-1,1]$

9. In any $\triangle ABC$ $rr_1r_2r_3 =$ ________

(A) $\triangle^4$ (B) $\triangle^3$ (C) $\triangle^2$ (D) $\triangle$

10. With usual notation $\sqrt{\frac{(s-b)(s-c)}{bc}}$ is equal to:

(A) $\cos\frac{\alpha}{2}$ (B) $\sin\frac{\alpha}{2}$ (C) $\sin\frac{\beta}{2}$ (D) $\sin\frac{\gamma}{2}$

11. $\cos^{-1}(-x)$ is equal to:

(A) $\frac{\pi}{2}-\sin^{-1}x$ (B) $\frac{\pi}{2}+\sin^{-1}x$ (C) $\pi+\cos^{-1}x$ (D) $\pi-\cos^{-1}x$

12. Solution of the equation $\tan x+1=0$ is:

(A) $\left\{\frac{3\pi}{4}+n\pi\right\}$ (B) $\left\{\frac{\pi}{4}+n\pi\right\}$ (C) $\{\pi+n\pi\}$ (D) $\{2\pi+n\pi\}$, when $n\in z$

13. If $z=a+ib$, what is the value of $\cos\theta$?

(A) $\frac{a}{|z|}$ (B) $\frac{b}{|z|}$ (C) $\frac{a}{b}$ (D) $\frac{b}{a}$

14. A function $f:A\to B$ is surjective if:

(A) Range $f=A$ (B) Range $f=B$ (C) Range $f\neq B$ (D) Range $f\neq A$

15. Determinant of any unit matrix has value:

(A) Greater than 1 (B) less than 1 (C) 1 (D) zero

16. A square matrix A is skew -symmetric if A^t is equal to:

(A) A (B) -A (C) A^t (D) A^2

17. The discriminant of $ax^2+bx+c=0$, $a\neq 0$ is:

(A) b^2+4ac (B) $4ac-b^2$ (C) b^2-4ac (D) a^2-4ac

18. The degree of the equation $x^3+3x^2+4x+5=0$ is

(A) 4 (B) 3 (C) 2 (D) 1

19. $\frac{x^2+1}{Q(x)}$ will be improper fraction if

(A) Degree of $Q(x)=2$ (B) Degree of $Q(x)=3$

(C) Degree of $Q(x)=4$ (D) Degree of $Q(x)=5$

20. $\sum_{K=1}^{n} K$ is equal to:

(A) $\frac{n+1}{2}$ (B) $\frac{n}{2}$ (C) $\frac{n(n+1)}{2}$ (D) $\frac{n(n-1)}{2}$

Roll No.________ to be filled in by the candidate.

(For all sessions)

Mathematics (Essay Type)

Time: 2:30 Hours **Marks: 80**

Section -I

2. Write short answers of any eight parts from the following. **2x8=16**

i. Separate into real and imaginary parts $\frac{i}{1+i}$.

ii. Simplify $\left(\frac{-1}{2}-\sqrt{3}/_{2}\,i\right)^3$.

iii. Write the converse and inverse of $q \to p$.

iv. Define the terms proper and improper subsets with example.

v. Find inverse of $\begin{bmatrix} -2 & 3 \\ -4 & 5 \end{bmatrix}$.

vi. Differentiate between I_n to and on to function.

vii. For a square matrix A, $|A| = |A^t|$.

viii. What is Rank of matrix? Explain with example.

ix. Solve $15x^2 + 2ax - a^2 = 0$ by quadratic formula.

x. If α, β are roots of $3x^2 - 2x + 4 = 0$, find $\frac{\alpha}{\beta} + \frac{\beta}{\alpha}$.

xi. Does the set $\{0, -1\}$ possess closure property w.r.t "Addition" and "multiplication"?

xii. Show that roots of equation $(p+q)x^2 - px - q = 0$ are rational.

3. Write short answers of any eight parts from the following. **2x8=16**

i. Resolve into partial fractions $\frac{x^2+1}{x^2-1}$.

ii. If $y = 1 + \frac{x}{2} + \frac{x^2}{4} + ...\infty$, show that $x = \frac{2(y-1)}{y}$.

iii. Prove that $\sum_{k=1}^{n} K = \frac{n(n+1)}{2}$.

iv. Find n, if ${}^{n}P_{2} = 30$.

v. Find n, if ${}^{n}C_{10} = \frac{12 \times 11}{2!}$.

vi. Define the probability.

vii. If 5 and 8 are arithematic means between a and b find a and b.

viii. Find 12th term of Harmonic progression $\frac{1}{3}, \frac{2}{9}, \frac{1}{6}$, ________

ix. In how many ways 4 keys be arranged on a circular key ring?

x. Prove the formula $1 + 3 + 5 + ... + (2n-1) = n^2$ for $n = 1, 2$.

xi. Find the term involving x^4 in the expansion of $(3-2x)^7$.

xii. Use binomial theorem, find the value to three decimal places $(1.03)^{\frac{1}{3}}$.

4. Write short answers of any nine parts from the following. **2x9=18**

i. Verify $2\sin 45^0 + \frac{1}{2}\operatorname{cosec}45^0 = 3/\sqrt{2}$.

ii. Prove that: $\frac{2\tan\theta}{1+\tan^2\theta} = 2\sin\theta\cos\theta$.

iii. Prove that $\tan\left(45^0+A\right)\tan\left(45^0-A\right)=1$.

iv. Prove that: $\dfrac{\sin 2\alpha}{1+\cos 2\alpha}=\tan\alpha$.

v. Define period of a trigonometric function.

vi. Prove that $\gamma=(s-a)\tan\dfrac{\alpha}{2}$.

vii. Prove that $\tan^{-1}\dfrac{1}{4}+\tan^{-1}\dfrac{1}{5}=\tan^{-1}\dfrac{9}{19}$.

viii. Solve $\sin x+\cos x=0$.

ix. Solve the trigonometric equation $\sec^2\theta=\frac{4}{3}$.

x. Find the radius of the circle in which the arm of the central angle of measure 1 radian cut off an arc of length 35cm.

xi. If α,β be the angle of a triangle ABC then prove that $\cos\left(\dfrac{\alpha+\beta}{2}\right)=\sin\frac{\gamma}{2}$.

xii. Find the smallest angle of ΔABC, when $a=37.34$, $b=3.24$, $c=35.06$.

xiii. Find area of triangle ABC given three sides $a=18$, $b=24$, $c=30$.

Section -II

Note: Attempt any three questions from the following. **10x3=30**

5. (a) Convert into logical form and prove by truth table of $(A\cap B)'=A'\cup B'$.

(b) Find the value of λ if given system has non-trivial solution

$$x_1+4x_2+\lambda x_3=0, 2x_1+x_2-3x_3=0, 3x_1+\lambda x_2-4x_3=0$$

6. (a) If α,β are the roots of $x^2-px-p-c=0$, then prove that: $(1+\alpha)(1+\beta)=1-C$.

(b) Resolve into partial fraction $\dfrac{x^2+a^2}{\left(x^2+b^2\right)\left(x^2+c^2\right)\left(x^2+d^2\right)}$

7. (a) The sum of 9 terms of a A.P is 171 and its eighth term is 31. Find the series.

(b) If x is very nearly equal 1 then prove that: $px^p-qx^q\simeq(p-q)x^{p+q}$.

8. (a) Find the value of remaining trigonometric function of $\sin\theta=-\dfrac{1}{\sqrt{2}}$ and the terminal arm of the angle is not in quad III.

(b) Prove that: $\dfrac{\sin 3\theta}{\cos\theta}+\dfrac{\cos 3\theta}{\sin\theta}=2\cot 2\theta$.

9. (a) Prove that: $r_1+r_2+r_3-r=4R$.

(b) Prove that: $\sin^{-1}\dfrac{3}{5}+\sin^{-1}\dfrac{8}{17}=\sin^{-1}\dfrac{77}{85}$.

☆ Inter. (Part-I)-A- 2019

Roll No.________ to be filled in by the candidate.	(For all sessions)	Paper Code	6	1	9	1

Mathematics (Objective Type)

Time: 30 Minutes **Marks: 20**

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A,B,C & D to each question are given.Which answer you consider correct, fill the corresponding circle A,B,C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. If $z=\cos\theta+i\sin\theta$, then $|z|$ is equal to:

(A) 0 (B) 1 (C) 2 (D) 3

2. For any two subsets A and B of set $\cup$, then $(A\cup B)'$ is equal to:

(A) $A\cup B'$ (B) $A\cap B'$ (C) $A'\cup B'$ (D) $A'\cap B'$

3. If "A" is a square matrix and $\left(\overline{A}\right)^t=-A$, then "A" is called:

(A) Skew Symmetric (B) Symmetric (C) Skew Hermitian (D) Hermitian

4. If $A=\begin{bmatrix}4 & x & 3\\ 7 & 3 & 6\\ 2 & 3 & 1\end{bmatrix}$ is a singular matrix, then 'x' is equal to:

(A) 3 (B) 4 (C) 6 (D) 7

5. If α and β are roots of $ax^2+bx+c=0$, then $\alpha.\beta$ is equal to:

(A) $-b/a$ (B) a/b (C) c/a (D) a/c

6. If "w" is a cube root of unity, then $\left(1+w-w^2\right)\left(1-w+w^2\right)$ will be equal to:

(A) 3 (B) 4 (C) 2 (D) 1

7. If $\dfrac{3}{(x-1)(x+2)}=\dfrac{1}{x-1}+\dfrac{A}{x+2}$, then "A" is equal to:

(A) -1 (B) 3 (C) 2 (D) 4

8. The n[th] root of product of n Geometric Means between a and b is equal to:

(A) $(ab)^{1/n}$ (B) a^nb^n (C) $n\sqrt{ab}$ (D) $\sqrt{ab}$

9. If in an A.P; $a_{n-3}=2n-5$, then a_n will be equal to:

(A) $2n+1$ (B) $2n-1$ (C) $n+1$ (D) $n-1$

10. $\dfrac{n!}{(n-r)!r!}$ is equal to:

(A) ${}^{r}C_{n}$ (B) ${}^{r}P_{n}$ (C) ${}^{n}C_{r}$ (D) ${}^{n}P_{r}$

11. Number of signals given by 5 flags of different colours using 3 flags at a time equals.

(A) 30 (B) 40 (C) 50 (D) 60

12. Sum of even co-efficient in the expansion of $(1+x)^n$ equals.

(A) 2^{n+1} (B) 2^{n-1} (C) 2^n (D) 2^{1-n}

13. Third term in the expansion of $(1-2x)^{1/3}$ is equal to:

(A) $-9x^2/4$ (B) $9x^2/4$ (C) $4x^2/9$ (D) $-4x^2/9$

14. The area of a sector of circular region of radius r and angle θ is equal to:

(A) $\frac{1}{2}r\theta^2$ (B) $\frac{1}{2}r^2\theta$ (C) $r\theta^2$ (D) $r^2\theta$

15. If $6\cos^2\theta + 2\sin^2\theta = 5$, then $\tan^2\theta$ will be equal to:

(A) $\frac{3}{2}$ (B) 3 (C) $\frac{1}{3}$ (D) $\frac{2}{3}$

16. Period of $\sin\frac{x}{5}$ is equal to:

(A) 10π (B) 5π (C) 2π (D) $\frac{2\pi}{5}$

17. In an oblique triangle, if $a = 200$; $b = 120$ and included angle $\gamma = 150^0$, then its area will be equal to:

(A) 6000 (B) 5000 (C) 2000 (D) 12000

18. If "R" is the circum-radius, then its value is:

(A) $\frac{ac}{4\Delta}$ (B) $\frac{ab}{4\Delta}$ (C) $\frac{abc}{4\Delta}$ (D) $\frac{abc}{\Delta}$

19. The value of $\sin\left(\cos^{-1}\frac{\sqrt{3}}{2}\right)$ is equal to:

(A) 1 (B) -1 (C) $\frac{-1}{2}$ (D) $\frac{1}{2}$

20. The solution of $\cos ec\theta = 2$ in interval $[0, 2\pi]$ is equal to:

(A) $\frac{\pi}{6}, \frac{7\pi}{6}$ (B) $\frac{\pi}{6}, \frac{5\pi}{6}$ (C) $\frac{\pi}{3}, \frac{5\pi}{6}$ (D) $\frac{\pi}{3}, \frac{\pi}{6}$

Roll No.________ *to be filled in by the candidate.* **(For all sessions)**

Mathematics (Essay Type)

Time: 2:30 Hours **Marks: 80**

Section -I

2. Write short answers of any eight parts from the following. **2x8=16**

i. Find the modulus of complex number $3+4i$.

ii. Simplify by justifying each step $\dfrac{\frac{1}{4}+\frac{1}{5}}{\frac{1}{4}-\frac{1}{5}}$ by writing properties.

iii. Factorize the expression $9a^2+16b^2$.

iv. Define absurdity and give one example.

v. Solve the system of linear equations. $\begin{matrix} 4x_1+3x_2=5 \\ 3x_1-x_2=7 \end{matrix}$

vi. Find the value of x if $\begin{vmatrix} 1 & 2 & 1 \\ 2 & x & 2 \\ 3 & 6 & x \end{vmatrix}=0$.

vii. Define Row Rank of a matrix.

viii. Solve the equation $x^{-2}-10=3x^{-1}$.

ix. If $A=\{1,2,3,4\}, B=\{3,4,5,6,7,8\}, C=\{5,6,7,9,10\}$ verify distributivity of union over intersection.

x. Find the inverse of the relation $\{(1,3),(2,5),(3,7),(4,9),(5,11)\}$.

xi. Use remainder theorem to find the remainder when x^3-x^2+5x+4 is divided by $x-2$.

xii. Find the roots of the equation $16x^2+8x+1=0$ by using quadratic formula.

3. Write short answers of any eight parts from the following. **2x8=16**

i. Resolve $\dfrac{1}{x^2-1}$ into partial fraction.

ii. Find 5th term of Geometric progression G.P 2,6,12,.......

iii. Define Circular permutation.

iv. Expand $(4-3x)^{\frac{1}{2}}$ upto three terms.

v. If $\frac{1}{a},\frac{1}{b},\frac{1}{c}$ are in Arithmatic progression (A.P) show that common difference is $\dfrac{a-c}{2ac}$.

vi. If 5,6 are two Arithmatic Means (A.M) between "a" and "b". Find "a" and "b".

vii. If the numbers $\frac{1}{k},\frac{1}{2k+1},\frac{1}{4k-1}$ are in (H.P) Hormonic Progression, Find "K".

viii. How many words can be formed from the letters of PLAN" using all letters when no letter is to be repeated?

ix. If ${}^{n}c_5={}^{n}c_4$, where c stands for combination then find value of n.

x. Verify the inequality $n>2^n-1$ for integral values of $n=4,5$.

xi. If x is so small that its square and higher power cab be neglected, show that $\dfrac{1-x}{\sqrt{1-x}}=1-\dfrac{3}{2}x$.

xii. Prove that Hormonic Mean (H.M) between two numbers "a" and "b" is $\dfrac{2ab}{a+b}$.

4. Write short answers of any nine parts from the following. **2x9=18**

i. Prove the fundamental identity $\cos^2\theta+\sin^2\theta=1$.

ii. Verify the result $\tan 2\theta=\dfrac{2\tan\theta}{1-\tan^2\theta}$ for $\theta=30^0$.

iii. Show that $\frac{\cos 11^0 + \sin 11^0}{\cos 11^0 - \sin 11^0} = \tan 56^0$.

iv. Prove that $\cos 330^0 \sin 600^0 + \cos 120^0 \sin 150^0 = -1$.

v. Find the period of $\operatorname{cosec}(10x)$.

vi. Show that $\gamma = 4R \sin\frac{\alpha}{2} \sin\frac{\beta}{2} \sin\frac{\gamma}{2}$ with usual notation.

vii. Find the value of $\cos\left(\sin^{-1}\frac{1}{2}\right)$.

viii. Show that $\frac{\cot^2\theta - 1}{1+\cot^2\theta} = 2\cos^2\theta - 1$.

ix. Exprss the following difference as the product of trignometric functions $\cos 7\theta - \cos\theta$.

x. In any triangle ΔABC, if $c = 16.1, \alpha = 42^0 45', \gamma = 74^0 32'$, then find "$\beta$" and "$\alpha$".

xi. Find the area of triangle ABC, given two sides and their included angle $a = 200, b = 120, \gamma = 150^0$.

xii. Find the solutions of the equation $\cot\theta = \frac{1}{\sqrt{3}}$ in the interval $[0, 2\pi]$.

xiii. Find the values of θ satisfying the equation $3\tan^2\theta + 2\sqrt{3}\tan\theta + 1 = 0$.

Section -II

Note: Attempt any three questions from the following. **10x3=30**

5. (a) Verify De Morgan's Laws for the given sets: $U = \{1,2,3,........20\}, A = \{2,4,6,......20\}, B = \{1,3,5,......19\}$.

(b) Find the value of λ if A is singular matrix, $A = \begin{bmatrix} 4 & \lambda & 3 \\ 7 & 3 & 6 \\ 2 & 3 & 1 \end{bmatrix}$.

6. (a) If the roots of $px^2 + qx + q = 0$ are α and β, then prove that $\sqrt{\frac{\alpha}{\beta}} + \sqrt{\frac{\beta}{\alpha}} + \sqrt{\frac{q}{p}} = 0$.

(b) Resolve into partial fraction $\frac{x^4}{1-x^4}$.

7. (a) The sum of an infinite geometric series is 9 and sum of square of its terms is $\frac{81}{5}$. Find the series.

(b) If $y = \frac{2}{5} + \frac{1.3}{2!}\left(\frac{2}{5}\right)^2 + \frac{1.3.5}{3!}\left(\frac{2}{5}\right)^3 + ...$, then prove that $y^2 + 2y - 4 = 0$.

8. (a) A railway train is running on a circular track of radius 500 meters at the rate of 30Km per hour. Through what angle will it turn in 10 sec?

(b) If $\tan\alpha = \frac{-15}{8}$ and $\sin\beta = \frac{-7}{25}$ and neither the terminal side of the angle of measure α nor that of β is in IV quadrant. Find $\sin(\alpha+\beta)$ and $\cos(\alpha+\beta)$.

9. (a) One side of a triangular garden is 30m. If two corner angle are $22^0\frac{1}{2}$ and $112^0\frac{1}{2}$, find the cost of planting the grass at the rate of Rs.5 per square meter.

(b) Prove that $\tan^{-1}\frac{3}{4} + \tan^{-1}\frac{3}{5} - \tan^{-1}\frac{8}{19} = \frac{\pi}{4}$.

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Roll No. ______ to be filled in by the candidate.

Inter. (Part-I)-A-2022

Mathematics (Objective Type)

(For all Sessions)

Paper Code | 6 | 1 | 9 | 6 |

Time: 30 Minutes **Marks: 20**

Note: You have four choices for each objective type question as A, B, C and D. The choice which you think is correct, fill that circle in front of that question number. Use marker or pen to fill the circles. Cutting or filling two more circles will result in zero mark in that question. Attempt as many questions as given in objective type question paper and leave others blank.

1.1. $\frac{\lfloor 3}{\lfloor 0} =$

(A) 0 (B) ∞ (C) 3 (D) 6

2. $^{n}C_{r}$ is valid only if.

(A) $r < n$ (B) $r > n$ (C) $r \le n$ (D) $r \ge n$

3. Sum of exponents of a and b in the expansion of $(a+b)^n$ in each term is.

(A) n (B) 2n (C) n^2 (D) $n+1$

4. End in the expansion of $\left(\frac{3x}{2} - \frac{1}{3x}\right)^{11}$ is ______.

(A) 5^{th} (B) 7^{th} (C) 4^{th} (D) 8^{th}

5. What angle is quadrental.

(A) 30° (B) 45° (C) 270° (D) 190°

6. $1 - Cos2\theta =$

(A) $2Sin^2\theta$ (B) $2Cos^2\theta$ (C) $2Sin^2 \theta/2$ (D) $2Cos^2 \theta/2$

7. Domain of Tangent function is $\mathbb{R}$ excluding. ______

(A) $\frac{n\pi}{2}$ (B) $2n\frac{\pi}{3}$ (C) $(2n+1)\pi$ (D) $(2n+1)\frac{\pi}{2}$

8. With usual notation. 2S -b = ______

(A) a − c (B) a + c (C) 2b+c (D) 2b+b+2c

9. Radius of e − circle is given by.

(A) $\frac{\Delta}{S-b}$ (B) $\frac{\Delta}{S+b}$ (C) $\frac{S-b}{\Delta}$ (D) $\frac{\Delta}{S+C}$

10. $x \ge +1$ or $x \le -1$ is the domain of.

(A) $Sin\,x$ (B) $Cos^{-1}\,x$ (C) $Sec^{-1}\,x$ (D) $Cot^{-1}\,x$

11. The solution of $\sin x + Cos\,x = 0$ in $[0, 2\pi]$

(A) $\frac{3\pi}{4}$ (B) $\frac{\pi}{4}$ (C) $\frac{\pi}{6}$ (D) $\frac{\pi}{3}$

12. Argument (θ) of $(\sqrt{3}+i)$ is.

(A) 60° (B) 30° (C) 45° (D) 90°

13. $\{1, \omega, \omega^2\}$ is group under.

(A) Addition (B) Subtraction (C) Multiplication (D) Intersection

14. For non singular matrices A and B $XA = B^{-1} \Rightarrow X =$

(A) $A^{-1}B$ (B) AB^{-1} (C) $(AB)^{-1}$ (D) $(BA)^{-1}$

15. If order of A is n x m and order of B is m x n then order of $(AB)^t$ is.

(A) n x m (B) m x m (C) m x n (D) n x n

16. If $4^{x} = \frac{1}{2}$ then $x =$

(A) $-\frac{1}{2}$ (B) −2 (C) $\frac{1}{2}$ (D) 2

17. If $x - a$ is a factor of $f(x)$, then for $f(x) = 0$ $x = a$ is.

(A) Root (B) Factor (C) Polynomial (D) Degree

18. Partial fraction of $\frac{1}{x^3+1}$ will be of the form.

(A) $\frac{A}{x+1} + \frac{B}{x^2+x+1}$ (B) $\frac{A}{x+1} + \frac{Bx+C}{x^2-x+1}$ (C) $\frac{A}{x+1} + \frac{Bx+C}{x^2+x+1}$ (D) $\frac{Ax+B}{x^2+1} + \frac{C}{x^2-x+1}$

19. Geometric series is convergent if.

(A) $|r| < 1$ (B) $|r| > 1$ (C) $|r| \le 1$ (D) $|r| \ge 1$

20. $\sum_{K=1}^{n} K^2 =$

(A) $\frac{n(n-1)(n-2)}{3}$ (B) $\frac{n(n-1)(n-2)}{6}$ (C) $\frac{n(n+1)(2n+1)}{3}$ (D) $\frac{n(n+1)(2n+1)}{6}$